

Suppression of Gravitational Structure Formation by Cosmological Accretion Heating

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ABSTRACT

As increasingly precise information about the spectrum of the cosmic microwave background fluctuations is gathered with balloon and satellite experiments, interest has grown in foreground sources of opacity affecting these observations. One potentially important source is electron scattering produced by a post-recombination luminosity source, which would significantly attenuate the higher harmonics in the spectrum. If such an ionization source exists, then it would also heat the universe, hence increasing the Jeans mass and suppressing early gravitational structure formation. Here we consider the effects of such heating. We concentrate on one type of ionization source: luminosity generated by accretion onto primordial compact objects. We show that if such objects generate enough luminosity to affect the CMB power spectrum, then they would produce enough heat to prevent the formation of 1σ collapsed objects until $z \sim 5$, significantly less than the redshift at which baryonic collapse could otherwise occur. Such processes would leave signatures detectable by upcoming instruments such as NGST, SIRTF, and SWIFT.

Subject headings: accretion, accretion disks — (cosmology:) cosmic microwave background — cosmology: theory — galaxies: formation

1. Introduction

The advent of a data-rich era in cosmology is expected to produce dramatically enhanced understanding of the early universe, from the initial spectrum of perturbations and their processing before radiation decoupling, to the formation of the first galaxies and stars. The high angular resolution power spectra of the cosmic microwave background (CMB) gathered by current and future satellite, balloon, and ground-based experiments are expected to provide precise information about many cosmological parameters, such as the total curvature of the universe and the baryonic mass fraction. These power spectra are also expected to be informative about a number of foreground sources, such as clusters of galaxies and other large-scale structure, and about the epoch of ionization of the intergalactic medium (e.g., Tegmark et al. 2000).

Early results from BOOMERanG and MAXIMA data suggested, surprisingly, that the second acoustic peak is significantly weaker than expected (de Bernardis et al. 2000; Hanany et al. 2000). More recent results from BOOMERanG (Netterfield et al. 2001), DASI (Pryke et al. 2001) and possibly MAXIMA (Lee et al. 2001) are consistent with the standard Λ CDM cosmology. However, the systematic uncertainties in current data are significant enough that it is still not possible to tell with precision whether the higher harmonics are at the expected amplitude; this will need to wait for instruments with absolute calibration such as MAP and Planck (e.g., Tegmark et al. 2000). Therefore, despite the encouraging agreement with expectations, it is worthwhile to calculate the impact that other effects have at both high and low redshifts.

The CMB spectrum can strongly constrain ionization at high redshifts, but some ionizing processes that may have only subtle effects (but nonetheless measurable with MAP and Planck) at $z \sim 1000$ can have important consequences at lower redshifts. One such effect within the standard model has been suggested recently by Peebles, Seager, & Hu (2000): if there exists a radiation source in the universe around the time of decoupling ($z \sim 1000$), the resulting enhanced density of free electrons at high redshift would Thomson scatter the CMB and suppress the second and higher peaks, in addition to moving the first acoustic peak to larger angular scales. Such sources could have many additional cosmological effects. In particular, if scattering is posited to suppress the second acoustic peak (Peebles et al. 2000) then the luminosity responsible for increased ionization would also heat the universe. As a result, the Jeans mass at early epochs would be raised, which in turn could affect the redshift of collapse of the first nonlinear structures.

One candidate for an early ionization source is accreting compact objects that exist by a redshift $z \sim 1000$, e.g., black holes formed during the quark-hadron phase transition. The first detailed investigation of the effects of such objects was performed by Carr (1981). He showed that the radiation generated by accretion of ambient gas onto primordial black holes could have a significant effect on the thermal and ionization history of the universe, potentially even preventing the universe from entering a neutral phase. Given large-amplitude baryonic fluctuations, massive black holes could have formed soon after recombination; Gnedin & Ostriker (1992) and Gnedin, Ostriker, & Rees (1995) considered the possible consequences for thermal, ionization, and nucleosynthesis histories of early injection of an AGN-like spectrum from such accreting sources.

An update to Carr's analysis was performed by Miller (2000), who used the existing limits on electron scattering optical depth between decoupling and the current epoch to place an upper bound on the contribution of primordial compact objects to dark matter. This limit is based on the effect such scattering would have on the angular power spectrum (limits based on distortions of the energy spectrum are much weaker; see, e.g., Griffiths, Barbosa, & Liddle 1999). Miller found that the product $\Omega_{\text{CO}}\epsilon_{-1}(M/10 M_\odot) < 4 \times 10^{-3}$ (in the notation of the current paper, $\xi < 4 \times 10^{-3}$), where Ω_{CO} is the fraction of closure density in compact objects, ϵ_{-1} is the accretion efficiency divided by 10%, and M is the typical mass of the compact object. In this paper we show that current data imply $\xi \lesssim 5 \times 10^{-4}$, which corresponds to a limit on optical depth that is three times stronger than used by Miller (2000) based on earlier data.

Here we explore the effect of ionizing sources on the gravitational structure formation history of the universe. We show that if accreting primordial compact objects generate enough ionization to significantly affect the second and third acoustic CMB peaks, then they raise the temperature of the universe to $T \gtrsim 500$ K when $z \lesssim 30$. As has been discussed by a number of authors (e.g., Ostriker & Gnedin 1996; Valageas & Silk 1999; Haiman, Abel, & Rees 2000; Gnedin 2000), an increase in temperature can dramatically alter the progress of structure formation. We show that in the present scenario, the Jeans instability threshold redshift for an $n - \sigma$ density fluctuation is reduced by $\sim 5 - 7$, compared to the threshold redshift when no extra heating sources are present. For example, $1 - \sigma$ fluctuations can collapse only at $z \approx 5$.

We find that the parameter $\xi = \Omega_{\text{CO}}\epsilon_{-1}(M/10 M_\odot)$ governs both the distorting effect on the CMB power spectrum and the formation of large-scale structure. Because the two effects are therefore linked, we do not need to assume anything about the accretion efficiency ϵ for the compact objects; instead, we may simply say that if accretion onto compact objects has a given effect on the CMB power spectrum, it will have a related (and much stronger) effect on the redshift at which nonlinear density peaks may form in baryons. If the accretion efficiency is low (e.g., if the flow is governed by an ADAF, CDAF, or wind-dominated solution, for which ϵ may be less than 10^{-4} ; see, e.g., Narayan, Mahadevan, & Quataert 1998; Ball, Narayan, & Quataert 2001; Blandford & Begelman 1999), all effects are proportionally reduced, but what we emphasize here is the relation between possible subtle effects at high redshift and significant effects at lower redshift.

In § 2 we calculate the ionization fraction produced by an accreting compact object beyond the immediate vicinity of the compact object (“HII region”) in the surrounding ambient region which contains many such objects. In order to allow for nonlinear mass concentrations, we generalize the analysis of Miller (2000) to include accretion in a region with density differing from the average density of the universe. In § 3 we compute the temperature of the HII and ambient regions by balancing accretion heating with Compton cooling off the CMB, also assessing the importance of bremsstrahlung, atomic cooling, and molecular cooling. In § 4 we determine the heating implied if Thomson scattering is responsible for reducing the second peak to presently-observed levels. We then evaluate the effect this level of heating would have on the formation of self-gravitating structures. In § 5, we discuss the effects of more general ionization and heating, and present our conclusions.

2. Ionization Fraction

In this section we focus on accreting primordial compact objects as the source of early ionization and heating. In § 5 we will revisit the heating effects of more general early ionization sources. The physical picture is of compact objects of typical mass M capturing matter via Bondi-Hoyle accretion from a surrounding medium. For generality we consider a medium with an ambient Hydrogen number density n_{amb} and temperature T_{amb} that may differ from the average

density \bar{n} and temperature \bar{T} of the universe. This will allow us to treat accretion in underdense or overdense mass concentrations. The luminosity generated by accretion will produce an HII region immediately around each compact object, in which the ionization fraction $x \approx 1$. Let the number density and temperature inside the HII region be n_{HII} and T_{HII} , respectively. As discussed by many authors (e.g., Silk 1971; Carr 1981; Miller 2000), the hardness of the spectrum produced by an accreting compact object implies that its ionization effect is felt over much greater distances than the radius of its Stromgren sphere, and the resulting ionization fraction decreases much more slowly with distance than is typical around an early-type star (as a power law, not exponentially).

Miller (2000) calculated the average ionization fraction for a differential luminosity spectrum typical of accreting black holes in our Galaxy, $dL(E)/dE \propto E^{-1} \exp(-E/E_{\max})$ (the range of spectra observed from stellar-mass black holes all give similar answers for the ionization fraction; see Miller 2000 for a more detailed discussion). Typically $E_{\max} \sim 100$ keV. Over a region large compared to the radius of the Stromgren sphere, the average ionization fraction at redshifts $z \lesssim 100$ is

$$\bar{x} \approx 3 \left[\frac{E_{\max}}{3E_0 \ln(E_{\max}/E_0)} \right]^{1/2} \left(\frac{R_s}{R_{\text{sep}}} \right)^{3/2}. \quad (1)$$

Here $E_0 = 13.6$ eV is the ground-state ionization energy of hydrogen and the number of compact objects per cosmological volume is $(4\pi R_{\text{sep}}^3/3)^{-1}$. In terms of the fraction Ω_{co} of closure density in compact objects and the redshift z ,

$$R_{\text{sep}} = 8 \times 10^{20} \text{ cm} (1+z)^{-1} \left(\frac{M}{10M_{\odot}} \right)^{1/3} \left(\frac{n_{\text{amb}}}{\bar{n}} \right)^{-1/3} \Omega_{\text{co}}^{-1/3}, \quad (2)$$

where we adopt $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$. The Stromgren radius is here defined as

$$R_s \equiv \left(\frac{2L}{3\pi\alpha n_{\text{amb}}^2 E_{\max}} \right)^{1/3}. \quad (3)$$

Here $\alpha = 1.5 \times 10^{-12} T_3^{-0.75} \text{ cm}^3 \text{ s}^{-1}$ is the recombination coefficient to the $n \geq 2$ states of hydrogen (Hummer 1994); recombination to the $n = 1$ state produces photons that are absorbed almost immediately, taking the standard “Case B” assumption. We scale the temperature as $T = 10^3 T_3$ K, because we find typical temperatures $T \sim 10^3$ K at the redshifts of interest. This form for the recombination coefficient is accurate to better than 10% for all $T > 10^2$ K, and to $\sim 1 - 2\%$ for $10^3 \text{ K} < T < 10^5$ K (Hummer 1994). The Bondi-Hoyle accretion rate is $\dot{M} = 4\pi\lambda_s(GM)^2\rho c_s^{-3}$, where for a $\gamma = 5/3$ gas the accretion eigenvalue is $\lambda_s = 0.25$. This produces a luminosity per source L given by

$$L \approx 3 \times 10^{27} \text{ erg s}^{-1} \epsilon_{-1} (1+z)^3 \left(\frac{M}{10M_{\odot}} \right)^2 \left(\frac{n_{\text{HII}}}{\bar{n}} \right) T_{\text{HII},3}^{-3/2}, \quad (4)$$

adopting a cosmological baryon density $\bar{\rho} = 3.6 \times 10^{-31} \text{ g cm}^{-3} (1+z)^3$ from Tytler et al (2000).

The accretion efficiency is defined as $L \equiv 0.1\epsilon_{-1}\dot{M}c^2$. The Stromgren radius is then

$$R_s \approx 4.4 \times 10^{19} \text{ cm} (1+z)^{-1} \epsilon_{-1}^{1/3} \left(\frac{E_{\max}}{10^4 E_0} \right)^{-1/3} \left(\frac{M}{10 M_\odot} \right)^{2/3} \left(\frac{n_{\text{HII}}}{\bar{n}} \right)^{1/3} \left(\frac{n_{\text{amb}}}{\bar{n}} \right)^{-2/3} T_{\text{HII},3}^{-1/2} T_{\text{amb},3}^{1/4}. \quad (5)$$

Pressure balance between the ambient medium and the HII region implies $n_{\text{HII}}T_{\text{HII}} = n_{\text{amb}}T_{\text{amb}}$. Collecting factors and defining $\xi \equiv \epsilon_{-1}(M/10M_\odot)\Omega_{\text{co}}$ as a parameter quantifying the generation of luminosity by accretion, the average ionization fraction in the ambient medium for $z \lesssim 100$ is

$$\bar{x} \approx 0.7 \xi^{1/2} \left[\frac{9}{\ln(E_{\max}/E_0)} \right]^{1/2} \left(\frac{T_{\text{amb}}}{T_{\text{HII}}} \right)^{7/8} T_{\text{HII},3}^{-3/8}. \quad (6)$$

The factor in brackets depends only on the spectrum, and is very close to unity. We note that the result from equations (1) and (6) is a factor $[8/\ln(E_{\max}/E_0)]^{1/2} \sim 1$ times the result obtained by equating the total ionization at a mean rate $n_{\text{co}}L/(3E_0)$ with recombinations at a mean rate $\alpha n_{\text{amb}}^2 x^2$. Because $L \propto n$ for energy generated via cosmic accretion, the resulting mean cosmic ionization is density independent except indirectly through the temperature.

3. Balance of Heating and Cooling

The formation of baryonic structure depends in part on whether the nonlinear mass at a given redshift exceeds the Jeans mass at that epoch. In § 4 we will derive the nonlinear mass. The Jeans mass depends on the typical temperature of the regions that may undergo collapse. We therefore need to compute this temperature in the presence of accretion heating and ionization.

The temperature T_{amb} of the ambient medium is determined by the balance of heating by accretion with cooling by a variety of processes. Since ionization is not perfectly efficient (i.e., only a fraction of available energy goes into ionization), heating by accretion is inevitable. Cooling depends on a number of processes; candidates include Compton cooling, bremsstrahlung, atomic recombination, and molecular cooling. In addition to considering ionization and thermal balance in the ambient medium, we must also evaluate the latter in the HII region. This is important because, at least for heating by accretion, the luminosity per compact object depends on both the temperature and the density inside the HII region (the Bondi radius is smaller than R_s for $M \lesssim 10^4 M_\odot$). We first compute the HII region and ambient temperatures T_{HII} , T_{amb} by balancing accretion heating and Compton cooling in each region separately, assuming pressure balance applies at the interface. We then demonstrate self-consistency by showing that if ionization is dominated by radiative ionization (as opposed to collisional ionization) then cooling by bremsstrahlung, atomic recombination, and formation of H_2 can be ignored. Only Compton cooling is effective.

Balance of accretion heating and Compton cooling. — In general, the heating rate is related to the ionization rate, with the heating rate per unit volume $\Gamma = \mathcal{E}_T \zeta (1-x)n_H$ for \mathcal{E}_T the typical excess (thermal) energy in each ionization, and ζ the ionization coefficient. As discussed by Carr

(1981), through ionization balance the heating rate may be related to the recombination rate as $\Gamma = \mathcal{E}_T \alpha x n_H n_e$. Numerically, the heating rate at $z \lesssim 100$ is thus

$$\Gamma \approx 6.2 \times 10^{-23} \text{ erg cm}^{-3} \text{ s}^{-1} x n_H n_e \left(\frac{\mathcal{E}_T}{2E_0} \right) T_3^{-0.75}, \quad (7)$$

where the number densities here (and everywhere else in this paper) are measured in cm^{-3} . Carr (1981) estimates that there is ≈ 7 eV of heating per ionization within the HII region, in which primarily soft photons interact due to their higher absorption cross sections. In the ambient medium far from the source, the soft photons have already been absorbed and hence the photons are harder. The number of ionizations per primary of energy E is then $\sim E/3E_0$ for typical photon energies ~ 1 keV or higher (Dalgarno, Yan, & Liu 1999), so that $\mathcal{E}_T \sim E(E/3E_0)^{-1} - E_0 = 2E_0$.

After decoupling but prior to structure formation the entire universe is nearly transparent to CMB photons. Scattering of these photons off of free electrons provides a volume cooling rate $4\sigma_T a T_{\text{CMB}}^4 k(T - T_{\text{CMB}}) n_e / (m_e c)$, or

$$\Lambda_{\text{CMB}} = 5.6 \times 10^{-33} \text{ erg cm}^{-3} \text{ s}^{-1} n_e (1+z)^4 (T_3 - T_{\text{CMB},3}). \quad (8)$$

At the redshifts $z \ll 1000$ relevant to our heating calculation, the temperature in the HII region or ambient medium is much greater than the temperature of the CMB and hence the factor in parentheses is approximately T_3 . Inside the HII region, we set n_H and n_e to n_{HII} , $x \approx 1$, and T to T_{HII} ; in the ambient region we set n_H to n_{amb} , n_e to $x n_{\text{amb}}$, and T to T_{amb} , and evaluate x from equation (6). From pressure balance with the surrounding ambient medium, $n_{\text{HII}} T_{\text{HII}} = n_{\text{amb}} T_{\text{amb}}$.

Equating the accretion heating and CMB Compton cooling rates (eqs. 7,8) in the HII region, we find

$$T_{\text{HII},3} = 10(1+z)^{-4/11} T_{\text{amb},3}^{4/11} \left(\frac{n_{\text{amb}}}{\bar{n}} \right)^{4/11} \left(\frac{\mathcal{E}_{\text{T,HII}}}{2E_0} \right)^{4/11}. \quad (9)$$

Similarly, thermal balance in the ambient region yields

$$T_{\text{amb},3} = 70(1+z)^{-4/7} \bar{x}^{4/7} \left(\frac{n_{\text{amb}}}{\bar{n}} \right)^{4/7} \left(\frac{\mathcal{E}_{\text{T,amb}}}{2E_0} \right)^{4/7}. \quad (10)$$

Combining this with our expressions from equation (6) for the ionization fraction \bar{x} in the ambient medium, and equation (9) for the temperature of the the HII region, we solve to obtain

$$T_{\text{amb},3} = 28(1+z)^{-2/5} \xi^{5/13} \left(\frac{n_{\text{amb}}}{\bar{n}} \right)^{2/5} \left(\frac{\mathcal{E}_T}{2E_0} \right)^{2/5} \left(\frac{9}{\ln(E_{\text{max}}/E_0)} \right)^{5/13}, \quad (11)$$

$$T_{\text{HII},3} = 33(1+z)^{-1/2} \xi^{1/7} \left(\frac{n_{\text{amb}}}{\bar{n}} \right)^{1/2} \left(\frac{\mathcal{E}_T}{2E_0} \right)^{1/2} \left(\frac{9}{\ln(E_{\text{max}}/E_0)} \right)^{1/7}, \quad (12)$$

and

$$\bar{x} = 0.19(1+z)^{3/11} \xi^{2/3} \left(\frac{n_{\text{amb}}}{\bar{n}} \right)^{-3/11} \left(\frac{\mathcal{E}_T}{2E_0} \right)^{-3/11} \left(\frac{9}{\ln(E_{\text{max}}/E_0)} \right)^{2/3}. \quad (13)$$

The exponents are not exact, but are close approximations to the formally derived exponents. We neglect possible differences between \mathcal{E}_T in the HII and ambient regions. Equations (11)–(13) apply at redshifts where $T \gg T_{\text{CMB}}$; as z approaches decoupling, the effects of accretion become negligible. Figure 1 shows the high-redshift ambient ionization boost for $\xi = 5 \times 10^{-4}$ (which we find in § 4.1 gives a good fit to the second-year BOOMERanG and DASI data), compared to the standard model in which there is no extra ionization and hence $\xi = 0$.

We now consider three other cooling mechanisms: atomic recombination, bremsstrahlung, and molecular cooling by formation of H_2 . For each of these we assume that the ionization fraction x is determined by the radiative ionization balance calculated earlier. In very dense or hot media, collisional ionization will raise the ionization fraction and therefore increase the effectiveness of these cooling mechanisms.

Atomic recombination.—In solving for the ionization fraction by equating the recombination rate with the radiative ionization rate we have already effectively taken atomic recombination cooling into account. This is because the thermal energy, $kT < 1$ eV, is much less than the ionization energy of 13.6 eV. Therefore, recombination plays a minor role in cooling the medium. If the temperature were high enough that collisional ionization were important, then recombination might play a major role, but here it can be neglected.

Bremsstrahlung.—The bremsstrahlung cooling rate is

$$\Lambda_{\text{brems}} = 4.4 \times 10^{-26} \text{ erg cm}^{-3} \text{ s}^{-1} x n_H n_e T_3^{1/2}. \quad (14)$$

The ratio of bremsstrahlung cooling to the heating rate is thus $\approx 6 \times 10^{-4} T_3^{5/4}$, which is small for the present situation.

Molecular cooling.—No metals are present in the early universe, so the only ways to form H_2 (by far the dominant molecule) are the two-stage processes (1) $H + e^- \rightarrow H^- + \gamma$ followed by $H^- + H \rightarrow H_2 + e^-$, and (2) $H^+ + H \rightarrow H_2^+ + \gamma$ followed by $H_2^+ + H \rightarrow H_2 + H^+$. Puy et al. (1993) give rates for these reactions, and (1) dominates by at least two orders of magnitude over the temperature range of interest. Moreover, the second step of process (1) is effectively instantaneous compared to the first, so the reaction rate for $H + e^- \rightarrow H^- + \gamma$ determines the overall rate of H_2 formation. This rate is $\alpha_{\text{mol}} = 10^{-15} \text{ s}^{-1} \text{ cm}^3 T_3$. Assuming as an upper bound that all ~ 10 eV released in this process escapes to infinity, the cooling rate in the (low-ionization) ambient medium is

$$\Lambda_{\text{mol}} = 10 \text{ eV} \times \alpha_{\text{mol}} n_e n_{\text{amb}}. \quad (15)$$

The ratio of this molecular cooling to the mean accretion heating is $2.7 \times 10^{-4} x^{-1} T_3^{7/4}$. From equations (11) and (13), this ratio becomes

$$\Lambda_{\text{mol}}/\Gamma = 0.5(1+z)^{-1} \left(\frac{n_{\text{amb}}}{\bar{n}} \right) \left(\frac{\mathcal{E}_{T,\text{amb}}}{2E_0} \right). \quad (16)$$

This is generally less than unity for the redshift range of interest, for regions that are not strongly overdense compared to the universe as a whole. Once a region becomes significantly condensed

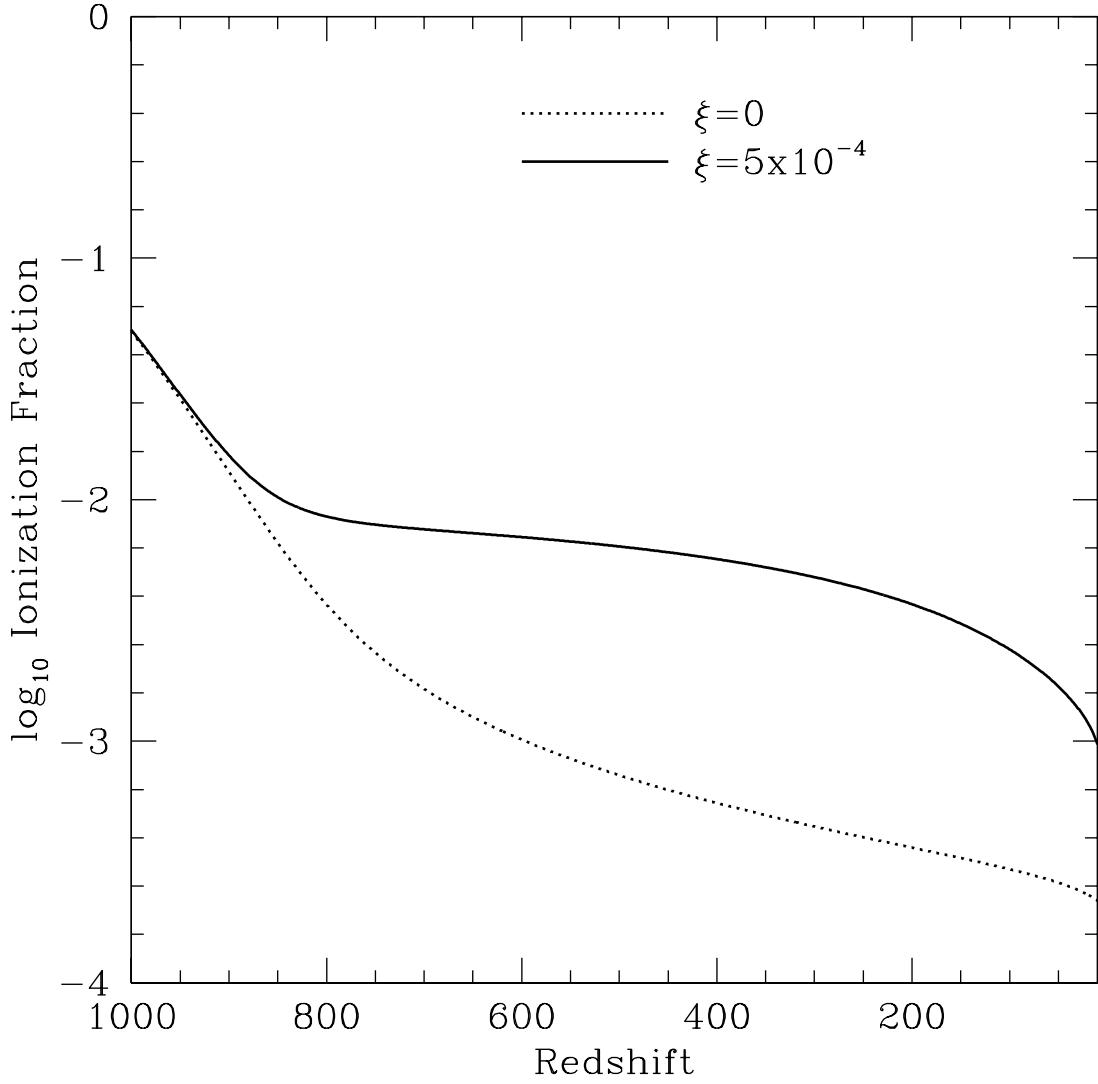


Fig. 1.— Fractional ionization x as a function of redshift, for accretion by primordial compact objects ($\xi = 5 \times 10^{-4}$, the best fit to the BOOMERanG and DASI data; see § 4.1), and for no extra ionization source ($\xi = 0$). Other cosmological parameters are chosen as in § 4.1. The relatively small difference at high redshifts implies that effects on the CMB power spectrum are small (albeit measurable), but the large difference at lower redshift is one consequence of the significant heating effect such sources can have during the epoch of nonlinear structure formation.

$(n_{\text{amb}}/\bar{n} \gg 1)$, molecular cooling begin to dominate other cooling terms (Lepp & Shull 1984). For the purposes of assessing the *onset* of collapse, however, we will simply use the result expressed in equation (11) obtained in the approximation that accretion heating and CMB Compton cooling are in balance.

4. Effects on the Formation of Structure

With the ambient temperature T_{amb} that we derived in the previous section, we can calculate the Jeans mass within a region of ambient density n_{amb} if we know the accretion parameter $\xi = \epsilon_{-1}(M/10 M_{\odot})\Omega_{\text{co}}$. We can then compare the Jeans mass as a function of redshift to the nonlinear mass scales at that redshift and hence evaluate, as a function of ξ , whether baryonic condensations within nonlinear dark matter peaks can collapse. In this section we first compute the maximum value of ξ compatible with current CMB data, then derive the nonlinear masses and determine the epoch of structure formation.

4.1. Relation to the CMB power spectrum

We use the code CMBFAST (version 4.0; Seljak & Zaldarriaga 1996 and subsequent papers) to generate a power spectrum and compare it to the best current signal to noise data, the second-year BOOMERanG (Netterfield et al. 2001) and DASI (Pryke et al. 2001) data. As an illustrative fit, we fixed all of the cosmological parameters except for ξ and then fit for ξ . We assume $\Omega_b = 0.05$, $\Omega_{\text{CDM}} = 0.29$, $\Omega_{\Lambda} = 0.66$ (and hence assume a flat universe), $\Omega_{\nu} = 0$, $H_0 = 66 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $T_{\text{CMB}}(z=0) = 2.726 \text{ K}$, $Y_{\text{He}} = 0.246$, three generations of massless neutrinos and none of massive neutrinos. These numbers are consistent with fits of recent CMB data that include priors based on large scale structure, Cepheid measurements of the Hubble constant, and Type Ia supernovae. This fit is also consistent with big bang nucleosynthesis. We also assume an $n = 1$ initial perturbation spectrum and adiabatic initial conditions, and do not include tensor perturbations. We included the additional ionization by modifying the routine “recfast.f”. At high redshift, the temperature of the HII region is no longer much greater than the temperature of the CMB, and hence for high z we solve for the ionization numerically without using this assumption.

We plot the resulting curves for no accretion ($\xi = 0$), $\xi = 5 \times 10^{-4}$, and $\xi = 10^{-3}$ against the second-year BOOMERanG and DASI data in Figure 2. The vertical bars are the estimated statistical uncertainties in measurement. Netterfield et al. (2001) estimate that there is a 20% systematic uncertainty in the points, and Pryke et al. (2001) estimate that there is a 16% uncertainty in the power measurements, but for this figure we have plotted the raw output from CMBFAST against the data, including only statistical errors. Note that there are also substantial systematic errors contributed by beam uncertainties, particularly for $\ell > 400$ (e.g., Netterfield et al. 2001), which have not been included in this figure. Clearly, the power spectrum is fairly

sensitive to ξ in this range. To get a rough idea of the goodness of fit, we made a simplistic comparison of the model with the data at the center of each ℓ range, allowing an overall shift up to $\pm 20\%$ but not varying the data to accommodate beam uncertainties. The resulting χ^2 values compared against the BOOMERanG data are: 39.1 for $\xi = 0$; 26.2 for $\xi = 5 \times 10^{-4}$; and 65.7 for $\xi = 10^{-3}$. In each case there are 17 degrees of freedom, since there are 19 data points and ξ and the overall scale are varied. The best value of $\xi = 5 \times 10^{-4}$ gives a fit acceptable at the 7% level, not including the beam errors, which make all of the curves significantly more compatible with the data. We note that the best-fit value of $\xi \equiv \epsilon_{-1}\Omega_{\text{co}}(M/10 M_\odot)$ is compatible with a low value of the accretion efficiency ϵ and/or a low value of the fraction of closure mass in compact objects Ω_{co} , provided the compact objects are relatively massive.

4.2. Growth of density perturbations

When density perturbations are linear, the relative amplitude $D(z)$ of a density perturbation $\delta = (\rho - \bar{\rho})/\bar{\rho}$ evolves with the overall scale factor $a \equiv (1 + z)^{-1}$ of the universe according to

$$D(z) = E(z) \frac{5\Omega_m}{2} \int_z^\infty \frac{1+z'}{E(z')^3} dz' \quad (17)$$

(Heath 1977). Here $E(z) = H(t)/H_0 = [\Omega_m(1+z)^3 + \Omega_r(1+z)^4 + \Omega_\Lambda + \Omega_k(1+z)^2]^{1/2}$, and Ω_m , Ω_r , Ω_Λ denote the present contributions to Ω from matter, radiation, and the cosmological constant, and $\Omega_k = 1 - (\Omega_m + \Omega_r + \Omega_\Lambda)$ is the overall curvature (our naming convention corresponds to that of, e.g., Peebles 1993). For the regime of interest, we shall neglect the Ω_r term. The power spectrum of small amplitude fluctuations at redshift z thus evolves under linear growth according to

$$P(k, z) = \left[\frac{D(z)}{D(0)} \right]^2 P_0(k), \quad (18)$$

where k is the comoving wavenumber of a fluctuation.

To obtain the power spectrum shape and normalization, we follow the development of Bunn & White (1997) and Hu & Sugiyama (1996). We assume that the power law slope of the initial perturbations is $n = 1$, that the universe is flat $\Omega_k = 0$, and that k , the comoving wavenumber, is measured in Mpc^{-1} . Bunn & White (1997) write the present-day power spectrum as $\Delta_0^2(k) = k^3 P_0(k)/2\pi^2 = \delta_H^2 \left(\frac{k}{H_0/c} \right)^{3+n} T^2(k)$, with $\delta_H \approx 2 \times 10^{-5} \Omega_m^{-0.73}$. The transfer function is given by (Bardeen et al. 1986)

$$T(q) = T \left(\frac{k}{h\Gamma} \right) = \frac{\ln(1 + 2.34q)}{2.34q} \left[1 + 3.89q + (16.1q)^2 + (5.46q)^3 + (6.71q)^4 \right]^{-1/4} \quad (19)$$

where $h\Gamma \approx \Omega_m h^2$. From Carroll, Press, & Turner (1992), a good approximation to the present growth factor is

$$D(0) \approx \frac{5\Omega_m}{2 \left[\Omega_m^{4/7} - \Omega_\Lambda + (1 + \Omega_m/2)(1 + \Omega_\Lambda/70) \right]}, \quad (20)$$

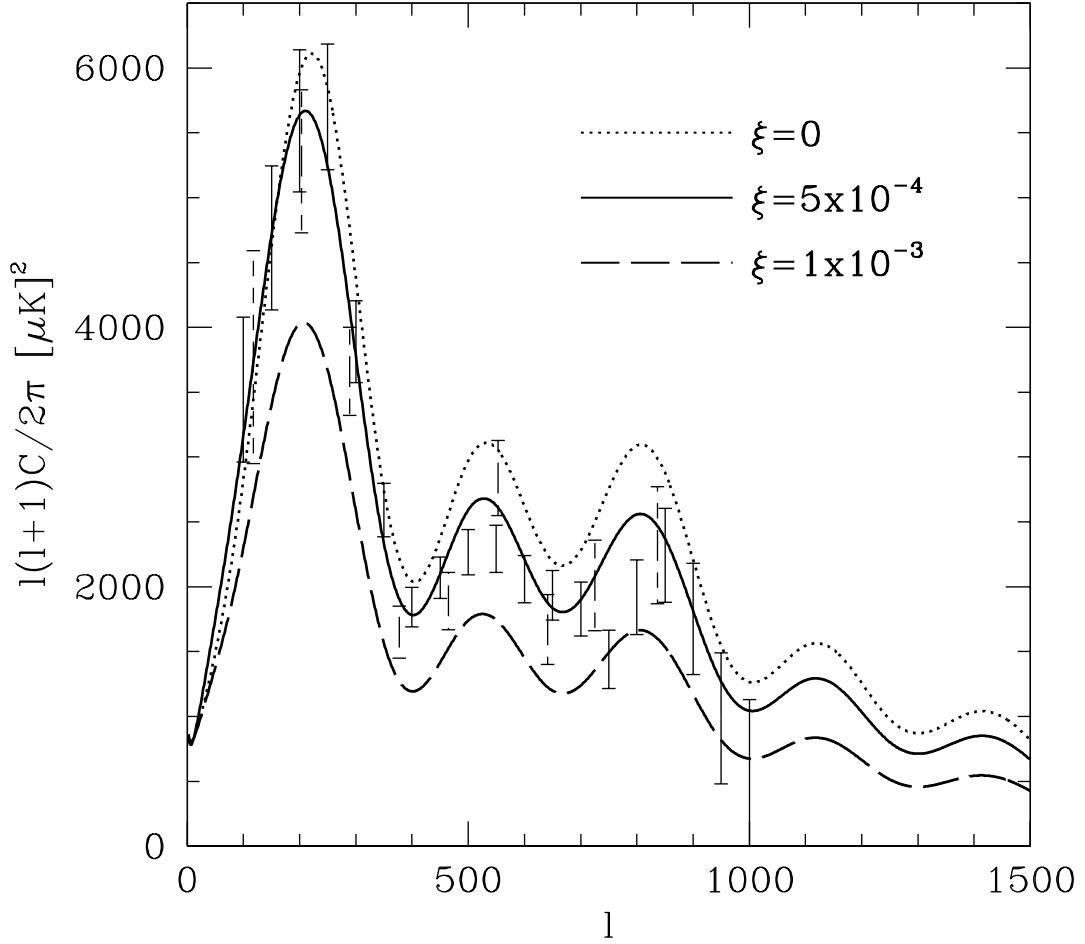


Fig. 2.— Comparison of CMBFAST output, using the compact object accretion model, to the second-year BOOMERanG data (Netterfield et al. 2001, solid error bars) and DASI data (Pryke et al. 2001, dashed error bars), including statistical but not systematic errors. Here only ξ is varied, and other cosmological parameters such as H_0 and Ω_Λ are fixed at the values indicated in the text. When a $\pm 20\%$ shift is allowed, $\xi = 0$ and $\xi = 5 \times 10^{-4}$ fit well, but $\xi = 10^{-3}$ still gives too low a first peak. Note that the amplitude of the second peak is quite sensitive to ξ . The best value, $\xi = 5 \times 10^{-4}$, gives an acceptable fit: for example, compared to the BOOMERanG data, $\chi^2 = 26.2$ for 17 degrees of freedom, including an overall systematic shift of 5% but not including beam errors.

so for $\Omega_m = 0.3$ and $\Omega_\Lambda = 0.7$, $D(0) \approx 0.8$.

The potential for collapsed objects of a given mass to form depends first of all on whether perturbations of the corresponding physical scale have grown sufficiently to become nonlinear. The variance in the fluctuation spectrum at a given mass M (or comoving length scale R) is related to the power spectrum at redshift z by the following equation (e.g. Barkana & Loeb 2000):

$$\sigma^2(M) = \sigma^2(R) = \int_0^\infty \frac{dk}{2\pi^2} k^2 P(k, z) \left[\frac{3j_1(kR)}{kR} \right]^2 ; \quad (21)$$

we adopt a top-hat filter $j_1(x) = (\sin x - x \cos x)/x^2$.

A top-hat perturbation on comoving scale R collapses in an Einstein-de Sitter universe at the point when its overdensity as predicted by *linear* theory reaches a value $\delta_c = 1.686$ (e.g. Peebles 1993); this critical overdensity has only a weak dependence on cosmological parameters. The typical redshift for a $1-\sigma$ peak at mass scale M to collapse is therefore given by the implicit solution of $\sigma(M) = \delta_c$ for z using equation (21); the collapse redshift for a mass scale M residing in a $2-\sigma$ peak is given by solution of $\sigma(M) = \delta_c/2$, and so on.

Whether the local baryons collapse into a given dark matter halo depends on the halo mass relative to the Jeans mass: baryons collapse with the halo only if the halo's gravitational potential ($\sim GM^{2/3}\rho^{1/3}$) exceeds the specific thermal energy of baryons ($\sim kT/\mu$). If we assume spherical density perturbations then the Jeans mass for a cloud of temperature T (and sound speed c_s) and total matter density ρ_{tot} (including both baryons and cold dark matter) is

$$M_J = \frac{1}{6}\pi\rho_{\text{tot}} \left(\frac{\pi c_s^2}{G\rho_{\text{tot}}} \right)^{3/2} \approx 7 \times 10^5 M_\odot (\rho_{\text{tot}}/\rho_{\text{amb}})^{-1/2} T_{\text{amb},3}^{3/2} n_{\text{amb}}^{-1/2} \quad (22)$$

for a cosmological abundance of helium. Here n_{amb} is measured in cm^{-3} and ρ_{amb} is the ambient density in baryons only. If we assume that during collapse the ratio of total mass to baryonic mass in a mass concentration remains approximately constant at the average value (roughly 9), then $(\rho_{\text{tot}}/\rho_{\text{amb}})^{-1/2} \approx 1/3$ and $M_J \approx 2 \times 10^5 M_\odot T_{\text{amb},3}^{3/2} n_{\text{amb}}^{-1/2}$. In the standard model, where there is no extra source of heating, the minimum halo mass for collapsed baryonic objects including shell crossing by dark matter and other effects is (Barkana & Loeb 2000)

$$M_{\text{min}} = 5 \times 10^3 M_\odot \left(\frac{1+z}{10} \right)^{3/2} \left(\frac{\Omega_m h^2}{0.15} \right)^{-1/2} \left(\frac{\Omega_b h^2}{0.022} \right)^{-3/5} , \quad (23)$$

which is almost identical to the value M_J , stand that the Jeans mass of equation (22) would take on in the absence of cosmic heating (see eq. 41 of Barkana & Loeb 2000). If instead heating by accretion *is* included, then from the results of the previous section we obtain

$$M_{J,\text{mod}} \approx 8 \times 10^{10} M_\odot (1+z)^{-2} \xi^{7/12} (n_{\text{amb}}/\bar{n})^{1/10} \approx 8 \times 10^8 M_\odot \xi^{7/12} [(1+z)/10]^{-2} . \quad (24)$$

Note that this mass is virtually independent of n_{amb} . Since $\xi \sim 5 \times 10^{-4}$ fits the BOOMERanG data, this implies $M_{J,\text{mod}} \approx 1.0 \times 10^7 M_\odot [(1+z)/10]^{-2}$. This mass is vastly greater than it would be sans heating, and hence has a major effect on structure formation.

Figure 3 exhibits this effect. Here we show, as a function of redshift, the nonlinear mass M_{nl} for 1- σ , 2- σ , and 3- σ peaks, along with the standard Jeans mass and the Jeans mass modified by accretion heating (with $\xi = 5 \times 10^{-4}$). The nominal collapse redshift for a given rarity of peak is significantly less than it would be without heating.

5. Discussion and Conclusions

We have shown that if accretion onto primordial compact objects produces enough luminosity to increase significantly the ionization fraction of the universe at $z \sim 1000$, then this luminosity has a dominant effect on the thermal evolution of the universe at lower redshifts. In particular, the Jeans mass is raised by some three orders of magnitude at $z \sim 10$, which would substantially delay baryonic structure formation. Even if the ionization produced by compact objects is insufficient to affect the second CMB acoustic peak strongly, the moderate dependence of the Jeans mass in equation (24) on the accretion luminosity parameter ξ implies that the presence of even a relatively small number of (evenly-distributed) primordial compact objects could have a strong effect on structure formation.

Effects on the observed cosmic background radiation other than on the power spectrum are very subtle. For example, the existence of extra free electrons with a temperature elevated above the radiation temperature will distort the photon energy spectrum. To first order this can be characterized by the Compton y parameter, $y = \int d\tau k\Delta T/m_e c^2$. However, even with the enhanced ionization and temperature, $y = 2 \times 10^{-9}$ when $\xi = 5 \times 10^{-4}$, compared with the limit $|y| < 7 \times 10^{-6}$ from COBE measurements (Mather et al. 1999). Thus, energy spectral distortions from scattering place far weaker limits on extra ionization than do limits to changes in the power spectrum (see also Griffiths et al. 1999). Another potential contributor to the energy spectrum is the luminosity from the accretion itself. However, this is also negligible. From equation (4), at $z \approx 10^3$ the luminosity per source is roughly $10^{36} \text{ erg s}^{-1} \epsilon_{-1} (M/10 M_\odot)^2$. The total luminosity is $L \approx 2 \times 10^{57} \text{ erg s}^{-1} \epsilon_{-1} \Omega_{\text{CO}} (M/10 M_\odot)^2 = 2 \times 10^{57} \text{ erg s}^{-1} \xi (M/10 M_\odot)$. Taking redshifts into account and assuming a radius of $\approx 10^{28} \text{ cm}$ for the universe, the observed flux would be $F \approx 2 \times 10^{-6} \xi \text{ erg cm}^{-2} \text{ s}^{-1}$. Even for $\xi = 1$ this is a factor of $\approx 10^3$ less than the flux from a 2.7 K blackbody. Taking into account that only a small fraction of the accretion radiation will be near the blackbody frequencies and that $\xi = 5 \times 10^{-4}$, the ratio of fluxes is $\approx 10^7$. The direct radiation is unobservable. Thus, at high redshift the power spectrum places the strongest limits on accretion by primordial compact objects. However, as we have shown, at low redshifts the effects can be much more dramatic.

An important difference between ionization by accreting primordial objects and ionization by, e.g., the first generation of stars or quasars is that the latter only exist after ordinary structure has already formed, whereas the former ionize and heat the universe independent of any structure formation. Hence, accretion onto primordial objects, or any other mechanism independent of structure formation at moderate redshift, can in principle delay any structure formation. Similar

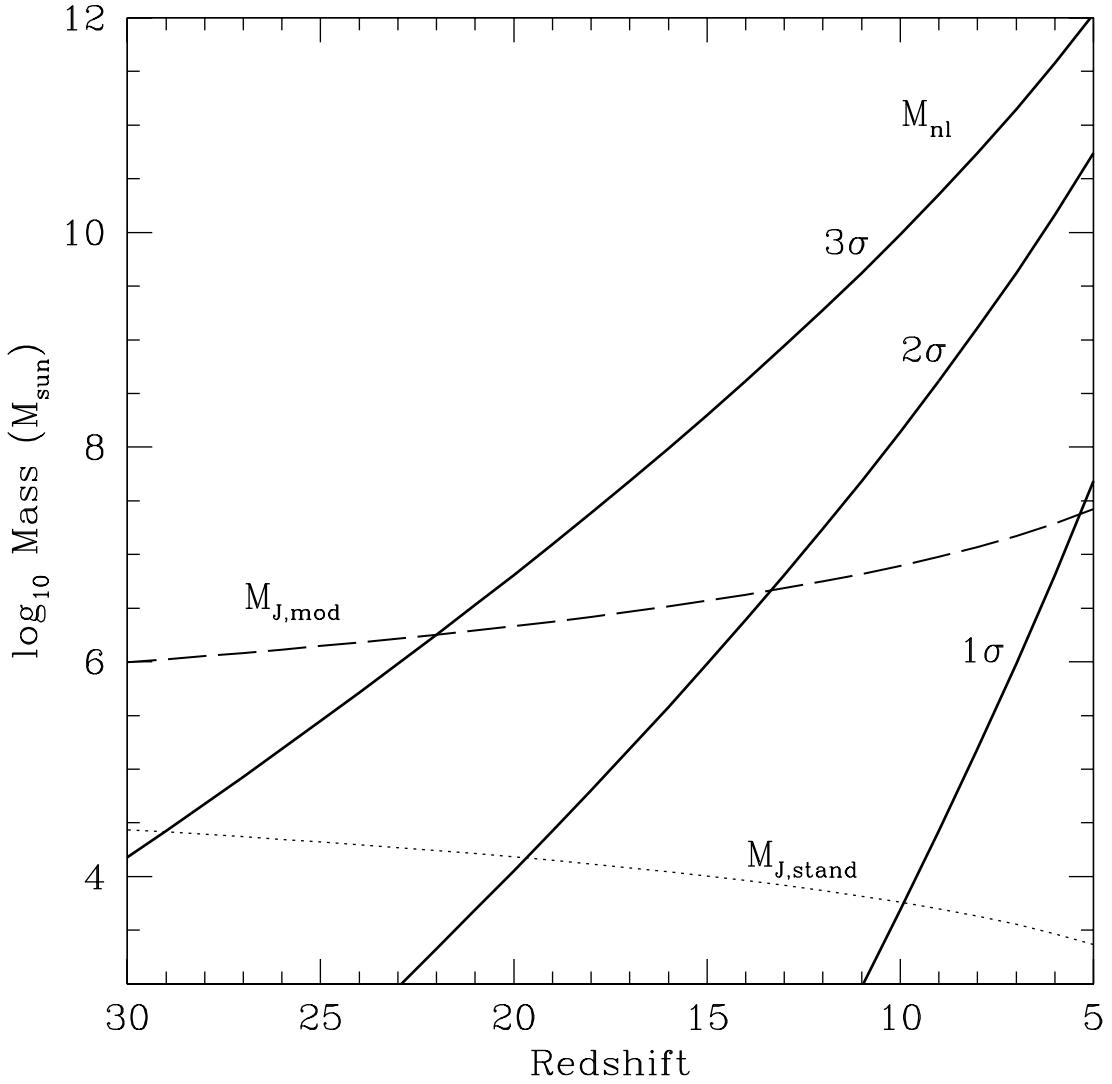


Fig. 3.— Nonlinear mass and Jeans mass as a function of redshift, with and without accretion heating. The solid lines show the nonlinear mass M_{nl} for 1σ , 2σ , and 3σ peaks. The dotted line ($M_{J,stand}$) is the Jeans mass assuming no additional heating, and the long dashed line ($M_{J,mod}$) is the Jeans mass modified by heating ($\xi = 5 \times 10^{-4}$) compatible with the most recent BOOMERanG, MAXIMA, and DASI data. This figure shows that the effect of such heating is to delay baryonic structure formation drastically; typically the formation redshift of an $n\sigma$ peak is 5-7 less than what it would be without the heating.

effects from early stars or quasars are self-limiting, and thus may not prevent – but nevertheless will regulate – further growth of structure (Ostriker & Gnedin 1996).

More generally, any ionization source will also heat the universe. For example, Peebles et al. (2000) analyzed a simple model in which a uniform source of Ly α photons exists early in the universe. More hydrogen atoms are therefore in the $n = 2$ state, so they can be ionized more easily. The enhanced ionization produces more free electrons, which scatter the CMB background, moving the surface of last scattering to lower redshift and therefore moving the first CMB peak to lower ℓ (larger angular scales) and decreasing the amplitude of the second CMB peak. In their model, they assume that the rate of production of Ly α photons per unit volume is

$$\frac{dn_\alpha}{dt} = \epsilon_\alpha n_H H(t) . \quad (25)$$

Here n_H is the number density of hydrogen, ϵ_α is a free parameter, and $H(t) = \dot{a}/a$ is the Hubble parameter at time t . Peebles et al. (2000) found that with this model, $\epsilon_\alpha = 10$ gave a good fit to the first-year BOOMERanG data.

Let us assume that for each Ly α photon produced by the sources there is some heating as well, and that the energy that heats the universe is a fraction f of the energy in the Ly α photons themselves. At moderate and high redshifts with $\Omega_m = 0.3$ and $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $H \approx 1.2 \times 10^{-18} \text{ s}^{-1}(1+z)^{3/2}$; the baryon density is $n_H = 1.5 \times 10^{-7} \text{ cm}^{-3}(1+z)^3$ from Tytler et al. (2000). The energy of a Ly α photon is approximately 10 eV, so the volume heating rate associated with equation (25) would be

$$\begin{aligned} \Gamma &= f\epsilon_\alpha(10 \text{ eV})n_H H(t) \\ &= 3 \times 10^{-36} \text{ erg cm}^{-3} \text{ s}^{-1} f\epsilon_\alpha(1+z)^{9/2} . \end{aligned} \quad (26)$$

From § 3, CMB cooling dominates over recombination and molecular cooling for the conditions of interest. If the ionization fraction is x and the temperature of the ambient medium is $10^3 T_{\text{amb},3} \text{ K}$, the cooling rate is

$$\Lambda_{\text{CMB}} = 1 \times 10^{-39} \text{ erg cm}^{-3} \text{ s}^{-1} x(1+z)^7 T_{\text{amb},3} . \quad (27)$$

Equating the two, the temperature is $T_{\text{amb},3} = 3000f\epsilon_\alpha x^{-1}(1+z)^{-5/2}$. If the hydrogen is completely ionized ($x = 1$), $\epsilon_\alpha = 10$ from Peebles et al (2000) implies a temperature of $1.5 \times 10^4 f \text{ K}$ at $z = 20$; reducing the ionized fraction raises the temperature. Thus, unless the generation of Ly α photons occurs almost free of heating ($f \ll 0.01$), the heating present if this source persisted at moderate redshift would raise the temperature dramatically above what it would be in the standard model, and hence increase the Jeans mass and delay structure formation. The only type of ionization source that could significantly affect the CMB power spectrum and yet not significantly affect structure formation is one with a very steep redshift dependence. If the energy generation rate per volume is $\epsilon \propto (1+z)^n$ with $n > 7$, heating effects at low redshift will be small. Otherwise, such heating will affect structure formation dramatically.

The richness of data available from upcoming cosmological experiments will rapidly establish whether such ionizing and heating sources exist. If, for example, the first nonlinear baryonic

objects did not form until $z \sim 15$ or more recently, evidence of this should be readily apparent in data from many future satellites, including NGST (see, e.g., Robinson & Silk 2000) and SIRTF (e.g., Fazio, Eisenhardt, & Huang 1999), and in the redshifts and absorption line spectra from distant gamma-ray bursts observed with HETE-2 and SWIFT (Wijers et al. 1998; Lamb & Reichart 2000; Blain & Natarajan 2000). In addition, as more data with better calibrations are available from CMB experiments, the effects at higher ℓ will be more sensitive to the presence of any extra ionization (Miller 2000). In either case, the role of extra ionizing and heating sources in the early universe will be clarified greatly in the next five years.

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